## Gyrosynchrotron Radiation

- → Expressions for the emission and absorption coefficient are much more complicated than the nonrelativistic (thermal gyroresonance) and ultra-relativistic (synchrotron) case, which are often solved numerically.
- → Gyrosynchrotron emission is typically produced by nonthermal electrons with energies of 100 keV~10 MeV.
- → Gyrosynchrotron emission is commonly observed as a broadband microwave spectrum in a typical frequency range of 2~20 GHz.
   Below 1 GHz it is self-absorbed and masked by free-free absorption from the overlying plasma.
- → The spectrum of gyrosynchrotron emission peaks typically around 5~10 GHz (3~6 cm), being optically thick at lower frequencies and optically thin at higher frequencies.

Dulk (1985)



Figure 15.2 in Markus J. Aschwanden (2005)

For a power-law electron spectrum (with slope  $\delta$  and electron number density N) which is isotropic in pitch angle,

gyrosynchrotron emissivity (or emission coefficient)  

$$\frac{\eta_{\nu}}{BN} \approx 3.3 \times 10^{-24} 10^{-0.52\delta} (\sin \theta)^{-0.43+0.65\delta} \left(\frac{\nu}{\nu_{\rm B}}\right)^{1.22-0.90\delta},$$
absorption coefficient  
 $\kappa_{\nu}B$ 

$$\frac{\kappa_{\nu} B}{N} \approx 1.4 \times 10^{-9} 10^{-0.22\delta} (\sin \theta)^{-0.09+0.72\delta} \left(\frac{v}{v_{\rm B}}\right) \qquad ,$$

effective temperature  

$$T_{\rm eff} \approx 2.2 \times 10^9 10^{-0.31\delta} (\sin \theta)^{-0.36-0.06\delta} \left(\frac{\nu}{\nu_{\rm B}}\right)^{0.50+0.085\delta},$$

 $v_{\text{peak}} \approx 2.72 \times 10^3 10^{0.27\delta} (\sin \theta)^{0.41 + 0.03\delta} (NL)^{0.32 - 0.03\delta} B^{0.68 + 0.03\delta}.$ 

brightness temperature  $T_b = T_{eff}(1 - e^{-\tau})$ 

 $\theta$ : angle between magnetic field and line-of-sight  $\mathcal{V}_B$ : electron gyrofrequency

valid over the range  $2 \le \delta \le 7$ ,  $\theta \ge 20^{\circ}$ , and  $10 \le v/v_{\rm B} \le 100$ 

Dulk (1985)

For thermal electrons (valid for all s > 5)

$$\begin{split} \frac{\kappa_{\rm v}B}{N_{\rm v}} &\approx 2.67 \times 10^{-9} \, \frac{\mu^2 (1-15/8\mu)}{n_{\sigma}^2 \sin^3 \theta} \, \frac{\gamma_{\rm o}^{3/2} (\gamma_{\rm o}^2-1)^{1/2}}{1+T_{\sigma}^2} \, \frac{\xi_{\rm o}^2 (\xi_{\rm o}^2-1)}{s_{\rm o}^{3/2} x^{1/2}} \\ &\times \left[ \left\{ c_2 (1+0.85s_{\rm c}/s_{\rm o})^{-1/3} + (1-n_{\sigma}^2\beta_{\rm o}^2)^{1/2} (1-n_{\sigma}^2\beta_{\rm o}^2 \cos^2 \theta)^{1/2} \right\}^2 \right. \\ &+ \frac{n_{\sigma}^2 \beta_{\rm o}^2 T_{\sigma}^2 \xi_{\rm o} \sin^4 \theta}{2(s_{\rm o}+s_{\rm c})} \right] (1-n_{\sigma}^2 \beta_{\rm o}^2 \cos^2 \theta) \left( 1+\frac{a_3 s_{\rm c}}{3 s_{\rm o}} \right)^{1/6} Z^{2s_{\rm o}} \\ &\times \exp\left[ -\mu(\gamma_{\rm o}-1) \right], \end{split}$$

where

$$\begin{split} \mu &= \frac{mc^2}{k_{\rm B}T}, \qquad \gamma_{\rm o} = \left[ 1 + \frac{2\nu}{\mu\nu_{\rm B}} \left( 1 + \frac{9x}{2} \right)^{-1/3} \right]^{1/2}, \\ \beta_{\rm o} &= \left( 1 - \frac{1}{\gamma_{\rm o}^2} \right)^{1/2}, \qquad x = \frac{\nu}{\nu_{\rm B}} \frac{\sin^2 \theta}{\mu}, \qquad n_{\sigma} \approx 1 - \frac{\nu_{\rm p}^2}{\nu^2}, \\ T_{\rm o} &= -T_{\rm x}^{-1} = -\left[ a + (1 + a^2)^{1/2} \right], \qquad a = \frac{\nu_{\rm B}}{\nu} \frac{\sin^2 \theta}{2 \cos \theta}, \\ s_{\rm o} &= \gamma_{\rm o} \frac{\nu}{\nu_{\rm B}} \left( 1 - n_{\sigma}^2 \beta_{\rm o}^2 \cos^2 \theta \right), \qquad a_3 = 13.589, \\ \xi_{\rm o} &= (1 - \beta'^2)^{-1/2}, \qquad \beta' = \frac{n_{\sigma} \beta_{\rm o} \sin \theta}{(1 - n_{\sigma}^2 \beta_{\rm o}^2 \cos^2 \theta)^{1/2}}, \\ s_{\rm c} &= \frac{3}{2} \xi_{\rm o}^3, \qquad c_2 = T_{\sigma} \cos \theta (1 - n_{\sigma}^2 \beta_{\rm o}^2), \qquad Z = \frac{\beta' e^{1/\xi_{\rm o}}}{1 + 1/\xi_{\rm o}}, \end{split}$$

Robinson & Melrose (1984)

For thermal electrons (valid for  $10^8 \le T \le 10^9$  K and  $10 \le s \le 100$ )

$$\begin{aligned} \frac{\kappa_{\nu}B}{N} &\approx 50T^{7} \sin^{6} \theta B^{10} \nu^{-10}, \\ \frac{\eta_{\nu}}{BN} &\approx 1.2 \times 10^{-24} T \left(\frac{\nu}{\nu_{B}}\right)^{2} \frac{\kappa_{\nu}B}{N}, \\ \nu_{\text{peak}} &\approx \begin{cases} 1.4 \left(\frac{NL}{B}\right)^{0.1} (\sin \theta)^{0.6} T^{0.7} B & (10^{8} < T < 10^{9} \text{ K}), \\ 475 \left(\frac{NL}{B}\right)^{0.05} (\sin \theta)^{0.6} T^{0.5} B & (10^{7} < T < 10^{8} \text{ K}). \end{cases} \end{aligned}$$



The optically-thin microwaves are more sensitive to electrons above 300 keV, while hard X-rays are usually dominated by electrons below 300 keV.