The control sequence $\forall r \in \mathsf{symbol} \mathcal{H}$, which is used mostly in superscripts. In fact, $\prime\prime$ is so big as it stands that you would never want to use it except in a subscript or superscript, where it occurs in a smaller size. Here are some typical examples:

prime tensor notation sqrt underline overline surds, see sqrt vinculum, see overline root

Input	Output
\$y_1^\prime\$	y_1'
<pre>\$y_2^{\prime\prime}\$</pre>	y_2''
<pre>\$y_3^{\prime\prime\prime}\$</pre>	$y_3^{\prime\prime\prime}$

Since single and double primes occur rather frequently, plain T_EX provides a convenient abbreviation: You can simply type ' instead of ^\prime, and '' instead of ^{\prime\prime}, and so on.

\$f'[g(x)]g'(x)\$	f'[g(x)]g'(x)
\$y_1'+y_2''\$	$y_1' + y_2''$
\$y'_1+y''_2\$	$y_1' + y_2''$
\$y'''_3+g'^2\$	$y_{3}^{\prime \prime \prime }+g^{\prime 2}$

Ś

▶ EXERCISE 16.5

Why do you think T_EX treats \prime as a large symbol that appears only in superscripts, instead of making it a smaller symbol that has already been shifted up into the superscript position?

► EXERCISE 16.6

Ş Mathematicians sometimes use "tensor notation" in which subscripts and superscripts are staggered, as in R_i^{jk} . Explain how to achieve such an effect.

Another way to get complex formulas from simple ones is to use the control sequences \sqrt, \underline, or \overline. Like ^ and _, these operations apply to the character or subformula that follows them:

\$\sqrt2\$	$\sqrt{2}$
\$\sqrt{x+2}\$	$\sqrt{x+2}$
\$\underline4\$	<u>4</u>
\$\overline{x+y}\$	$\overline{x+y}$
<pre>\$\overline x+\overline y\$</pre>	$\overline{x} + \overline{y}$
<pre>\$x^{\underline n}\$</pre>	$x^{\underline{n}}$
<pre>\$x^{\overline{m+n}}\$</pre>	$x^{\overline{m+n}}$
\$\sqrt{x^3+\sqrt\alpha}\$	$\sqrt{x^3 + \sqrt{\alpha}}$

You can also get cube roots ' $\sqrt[3]{}$ ', and similar things by using \root:

\$\root 3 \of 2\$		$\sqrt[3]{2}$
$\ \ \ \ \ \ \ \ \ \ \ \ \ $	`n+y^n}\$	$\sqrt[n]{x^n + y^n}$
\$\root n+1 \of a	1\$	$\sqrt[n+1]{a}$

Appendix F lists many more binary operations, for which you type control sequences instead of single characters. Here are some examples:

$x\times y\cdot z$
$x \circ y \bullet z$
$x\cup y\cap z$
$x \sqcup y \sqcap z$
$x \vee y \wedge z$
$x\pm y\mp z$

It is important to distinguish \times (\times) from X (X) and from x (x); to distinguish \cup (\cup) from U (U) and from u (u); to distinguish \vee (\vec{vee}) from V (V) and from v (v); to distinguish \circ (\circ) from O (0) and from o (o). The symbols ' \vee ' and ' \wedge ' can also be called \lor and \land, since they frequently stand for binary operations that are called "logical or" and "logical and."

 \sum Incidentally, binary operations are treated as ordinary symbols if they don't occur between two quantities that they can operate on. For example, no extra space is inserted next to the +, -, and * in cases like the following:

\$x=+1\$	x = +1
\$3.142-\$	3.142 -
\$(D*)\$	(D*)

Consider also the following examples, which show that binary operations can be used as ordinary symbols in superscripts and subscripts:

\$K_n^+,K_n^-\$	K_n^+, K_n^-
\$z^*_{ij}\$	z_{ij}^*
<pre>\$g^\circ \mapsto g^\bullet\$</pre>	$g^{\circ} \mapsto g^{ullet}$
\$f^*(x) \cap f_*(y)\$	$f^*(x) \cap f_*(y)$

times cup vee circ cdot bullet cap sqcup sqcap wedge cross, see dagger, times $_{\rm pm}$ mp lor land logical or logical and relations le ne simeq colon equals lessthan greaterthan colonequals equiv not subset subseteq simhooks, see subset, supset

wiggle, see sim

EXERCISE 16.11

Ş

How would you obtain the formulas z^{*2} , and $h'_{*}(z)$?

Plain T_EX treats the four characters =, <, >, and : as "relations" because they express a relationship between two quantities. For example, 'x < y' means that x is less than y. Such relationships have a rather different meaning from binary operations like +, and the symbols are typeset somewhat differently:

\$x=y>z\$	x = y > z
\$x:=y\$	x := y
\$x\le y\ne z\$	$x \leq y \neq z$
\$x\sim y\simeq z\$	$x \sim y \simeq z$
\$x\equiv y\not\equiv z\$	$x\equiv y\not\equiv z$
\$x\subset y\subseteq z\$	$x \subset y \subseteq z$

(The last several examples show some of the many other relational symbols that plain T_EX makes available via control sequences; see Appendix F.)

 T_EX doesn't know that you forgot a '\$' after the first 'n', because it doesn't understand English; so it finds a "formula" between the first two \$ signs:

The smallest nsuch that

after which it thinks that '2' is part of the text. But then the $\hat{}$ reveals an inconsistency; T_EX will automatically insert a \$ before the $\hat{}$, and you will get an error message. In this way the computer has gotten back into synch, and the rest of the document can be typeset as if nothing had happened.

If for some reason you cannot use $\hat{}$ and $_$ for superscripts and subscripts, because you have an unusual keyboard or because you need $\hat{}$ for French accents or something, plain TEX lets you type \sp and \sb instead. For example, ' $x \ge 2$ ' is another way to get ' x^2 '. On the other hand, some people are lucky enough to have keyboards that contain additional symbols besides those of standard ASCII. When such symbols are available, TEX can be set up to make math typing a bit more pleasant. For example, at the author's installation there are keys labeled \uparrow and \downarrow that produce visible symbols (these make superscripts and subscripts look much nicer on the screen); there are keys for the relations \leq , \geq , and \neq (these save time); and there are about two dozen more keys that occasionally come in handy. (See Appendix C.)

Mathematicians are fond of using accents over letters, because this is often an effective way to indicate relationships between mathematical objects, and because it greatly extends the number of available symbols without increasing the number of necessary fonts. Chapter 9 discusses the use of accents in ordinary text, but mathematical accents are somewhat different, because spacing is not the same; T_EX uses special conventions for accents in formulas, so that the two sorts of accents will not be confused with each other. The following math accents are provided by plain T_FX :

\$ <mark>\hat</mark> a\$	\hat{a}
\$ <mark>\check</mark> a\$	ă
\$ <mark>\tilde</mark> a\$	\tilde{a}
\$ <mark>\acute</mark> a\$	\acute{a}
\$ <mark>\grave</mark>) a\$	à
\$ <mark>\dot</mark> a\$	\dot{a}
\$ <mark>\ddot</mark> a\$	\ddot{a}
\$ <mark>\breve</mark> a\$	ă
\$ <mark>\bar</mark> a\$	\bar{a}
\$ <mark>\vec</mark> a\$	\vec{a}

The first nine of these are called $\, v, \langle v, \langle \cdot, \langle \cdot, \rangle, u$, and $\langle =$, respectively, when they appear in text; $\vee ec$ is an accent that appears only in formulas. T_EX will complain if you try to use \uparrow or $\vee v$, etc., in formulas, or if you try to use $\wedge hat$ or $\wedge check$, etc., in ordinary text.

par \mathbf{sp} \hat{sb} character set uparrow downarrow lea geq neq accents hat check tilde acute grave dot ddot breve bar vec

Now that the font layouts have all been displayed, it's time to consider the names of the various mathematical symbols. Plain T_EX defines more than 200 control sequences by which you can refer to math symbols without having to find their numerical positions in the layouts. It's generally best to call a symbol by its name, for then you can easily adapt your manuscripts to other fonts, and your manuscript will be much more readable.

The symbols divide naturally into groups based on their mathematical class (Ord, Op, Bin, Rel, Open, Close, or Punct), so we shall follow that order as we discuss them. N.B.: Unless otherwise stated, math symbols are available only in math modes. For example, if you say '\alpha' in horizontal mode, T_EX will report an error and try to insert a \$ sign.

1. Lowercase Greek letters.

α	\alpha	ι	\iota	ϱ	\varrho
β	\beta	κ	\kappa	σ	∖sigma
γ	\gamma	λ	\lambda	ς	\varsigma
δ	\delta	μ	\mu	au	\tau
ϵ	\epsilon	ν	\nu	v	\upsilon
ε	\varepsilon	ξ	\xi	ϕ	\phi
ζ	\zeta	0	0	φ	∖varphi
η	\eta	π	\pi	χ	∖chi
θ	\theta	ϖ	\varpi	ψ	\psi
ϑ	\vartheta	ρ	\rho	ω	∖omega

There's no **\omicron**, because it would look the same as **o**. Notice that the letter **\upsilon** (v) is a bit wider than **v** (v); both of them should be distinguished from **\nu** (v). Similarly, **\varsigma** (ς) should not be confused with **\zeta** (ζ). It turns out that **\varsigma** and **\upsilon** are almost never used in math formulas; they are included in plain T_EX primarily because they are sometimes needed in short Greek citations (cf. Appendix J).

2. Uppercase Greek letters.

Γ \Gamma	Ξ \Xi	$\Phi \setminus \texttt{Phi}$
Δ \Delta	Π \Pi	$\Psi \setminus \texttt{Psi}$
Θ \Theta	Σ \Sigma	$\Omega \setminus \texttt{Omega}$
Λ \Lambda	$\Upsilon \setminus Upsilon$	

The other Greek capitals appear in the roman alphabet (\Alpha \equiv {\rm A}, \Beta \equiv {\rm B}, etc.). It's conventional to use unslanted letters for uppercase Greek, and slanted letters for lowercase Greek; but you can obtain ($\Gamma, \Delta, \ldots, \Omega$) by typing \$({\mit\Gamma}, {\mit\Delta}, \ldots, {\mit\Omega})\$.

3. Calligraphic capitals. To get the letters $\mathcal{A} \dots \mathcal{Z}$ that appear in Figure 5, type $\{ cal A} \ z \$. Several other alphabets are also used with mathematics (notably Fraktur, script, and "blackboard bold"); they don't come with plain T_EX , but more elaborate formats like \mathcal{AMS} - T_EX do provide them.

symbols in math, table alpha iota varrho beta kappa sigma gamma lambda varsigma delta mu tau epsilon nu upsilon varepsilon xi phi zeta varphi eta $_{\rm pi}$ chi theta varpi psivartheta rho omega omicron Gamma Xi Phi Delta Pi Psi Theta Sigma Omega Lambda Upsilon Alpha Beta mit calligraphic letters Fraktu script blackboard bold

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4. Miscelle	aneous symbols of type	Ord			
Я	\aleph	1	\prime	\forall	\forall
\hbar	\hbar	Ø	\emptyset	Ξ	\exists
\imath	\imath	∇	<mark>\nabla</mark>	_	\neg
J	\jmath		\surd	þ	\flat
ℓ	\ell	Т	\top	þ	\natural
Ş	\wp	\perp	\bot	#	\sharp
\Re	\Re		\mathbf{M}	÷	\clubsuit
\Im	\Im	Z	\angle	\diamond	\diamondsuit
∂	\partial	\triangle	\triangle	\heartsuit	\heartsuit
∞	\infty	\	\backslash	٨	\spadesuit

5. Digits. To get italic digits 0123456789, say {\it0123456789}; to get boldface digits 0123456789, say {\bf0123456789}; to get oldstyle digits 0123456789, say {\oldstyle0123456789}. These conventions work also outside of math mode.

6. "Large" operators. The following symbols come in two sizes, for text and display styles:



It is important to distinguish these large Op symbols from the similar but smaller Bin symbols whose names are the same except for a 'big' prefix. Large operators usually occur at the beginning of a formula or subformula, and they usually are subscripted; binary operations usually occur between two symbols or subformulas, and they rarely are subscripted. For example,

 $\frac{1}{n}(x_n \cup y_n)$ yields $\bigcup_{n=1}^m (x_n \cup y_n)$

The large operators \sum , \prod , \coprod , and \int should also be distinguished from smaller symbols called Σ (Σ), Π (Π), \mbox{amalg} (Π), and \smallint (\int), respectively; the \smallint operator is rarely used.

aleph prime forall hbar emptyset exists imath nabla neg jmath surd flat elltop natural wp bot sharp Re escvert clubsuit Im angle diamondsuit partial . triangle heartsuit infty backslash spadesuit Weierstrass, see wp dotless letters accent digits sum bigcap bigodot prod bigcup bigotimes coprod bigsqcup bigoplus int bigvee biguplus oint bigwedge binary operations smallint

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7. Binary operations. Besides + and -, you can type

\pm \pm	∩ \cap	∨ \vee
$\mp \mbox{mp}$	\cup \cup	\land \wedge
\setminus \setminus	⊎ \uplus	🕀 📏 oplus
• <mark>\cdot</mark>	□ \sqcap	⊖ ∖ominus
× <mark>\times</mark>	∐ \sqcup	🚫 📏 otimes
* \ast	⊲ \triangleleft	\oslash \oslash
* \star	▷ \triangleright	💽 <mark>\odot</mark>
\diamond \diamond	<pre>> \wr</pre>	† \dagger
○ \circ	\bigcirc \bigcirc	‡ \ddagger
• \bullet	$ riangle$ \bigtriangleup	\amalg \amalg
÷ \div	\bigtriangledown \bigtriangledown	

It's customary to say $G\backslash H$ to denote double cosets of G by $H(G \setminus H)$, and $p\backslash n$ to mean that p divides $n(p \setminus n)$; but $X\setminus Y$ denotes the elements of set X minus those of set $Y(X \setminus Y)$. Both operations use the same symbol, but backslash is type Ord, while setminus is type Bin (so T_EX puts more space around it).

8. Relations. Besides <, >, and =, you can type



The symbols \mid and \parallel define relations that use the same characters as you get from | and \|; T_EX puts space around them when they are relations.

9. Negated relations. Many of the relations just listed can be negated or "crossed out" by prefixing them with \not, as follows:

, XXXXV	<pre>\not< \not\leq \not\prec \not\preceq \not\subset \not\subseteq \not\subseteq</pre>	, XXXAA	<pre>\not> \not\geq \not\succ \not\succeq \not\supset \not\supseteq \not\supseteq</pre>	,≢≁≄≉≇	<pre>\not= \not\equiv \not\sim \not\simeq \not\approx \not\cong \not\cong \not\asymp</pre>
¥	\not\sqsubseteq	⊉	\not\sqsupseteq	\neq	\not\asymp

pmcap vee $^{\mathrm{mp}}$ cup wedge setminus uplus oplus cdot sqcap ominus times sqcup otimes ast triangleleft oslash star triangleright odotdiamond wr dagger circ bigcirc ddagger bullet bigtriangleup amalg div bigtriangledown leq geq equiv prec SHCC approx preceq succeq propto Ĩ1 $\mathbf{g}\mathbf{g}$ asymp subset supset \sin subseteq supseteq simeq sqsubseteq sqsupseteq cong $_{\mathrm{in}}$ ni bowtie vdash dashv models \mathbf{smile} mid doteq frown parallel perp

not

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The symbol **\not** is a relation character of width zero, so it will overlap a relation that comes immediately after it. The positioning isn't always ideal, because some relation symbols are wider than others; for example, **\not\in** gives ' \notin ', but it is preferable to have a steeper cancellation, ' \notin '. The latter symbol is available as a special control sequence called **\notin**. The definition of **\notin** in Appendix B indicates how similar symbols can be constructed.

10. Arrows. There's also another big class of relations, namely those that point:

$\leftarrow \$ leftarrow	\leftarrow \longleftarrow	Î	\uparrow
$\Leftarrow \ \$	\leftarrow \Longleftarrow	↑	\Uparrow
ightarrow	$\longrightarrow \longrightarrow$	\downarrow	\downarrow
$\Rightarrow $ \Rightarrow	\implies \Longrightarrow	₩	\Downarrow
$\leftrightarrow \ leftrightarrow$	\longleftrightarrow \longleftrightarrow	Ĵ	\updownarrow
$\Leftrightarrow \$ Leftrightarrow	$\iff \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$	İ	\Updownarrow
$\mapsto \mbox{mapsto}$	$\longmapsto \texttt{longmapsto}$	7	\nearrow
 ← \hookleftarrow 	$\hookrightarrow \land$ hookrightarrow	\mathbf{n}	\searrow
$\leftarrow \$ leftharpoonup	\rightarrow \rightharpoonup	1	\swarrow
\leftarrow \leftharpoondown	\rightarrow \rightharpoondown	5	\nwarrow
\rightleftharpoons \rightleftharpoons			

Up and down arrows will grow larger, like delimiters (see Chapter 17). To put symbols over left and right arrows, plain T_EX provides a **buildrel** macro: You type **buildrel**(superscript)**over**(relation), and the superscript is placed on top of the relation just as limits are placed over large operators. For example,

(In this context, '\over' does not define a fraction.)

11. Openings. The following left delimiters are available, besides '(':

[\lbrack	\lfloor	[\lceil
{ \lbrace	\langle \langle	

You can also type simply '[' to get \lbrack. All of these will grow if you prefix them by \bigl, \Bigl, \biggl, or \left. Chapter 17 also mentions \lgroup and \lmoustache, which are available in sizes greater than \big. If you need more delimiters, the following combinations work reasonably well in the normal text size:

\lbrack\!\lbrack 《 \langle\!\langle ((\!(

12. Closings. The corresponding right delimiters are present too:

] \rbrack	\rfloor] \rceil
<pre>} \rbrace</pre>	<pre>> \rangle</pre>	

Everything that works for openings works also for closings, but reversed.

notin arrows leftarrow longleftarrow uparrow Leftarrow Longleftarrow Uparrow rightarrow longrightarrow downarrow Rightarrow Longrightarrow Downarrow leftrightarrow longleftrightarrow updownarrow Leftrightarrow Longleftrightarrow Updownarrow mapsto longmapsto nearrow hookleftarrow hookrightarrow searrow leftharpoonup rightharpoonup swarrow leftharpoondown rightharpoondown nwarrow rightleftharpoons buildrel over left delimiters lbrack lbrace langle lfloor lceil bigl Bigl biggl Biggl left lgroup lmoustache rbrack rbrace rangle rfloor rceil

13. Punctuation. T_EX puts a thin space after commas and semicolons that appear in mathematical formulas, and it does the same for a colon that is called **\colon**. (Otherwise a colon is considered to be a relation, as in 'x := y' and 'a : b :: c : d', which you type by saying 'x := y\$' and 'a : b :: c : d'.) Examples of **\colon** are

$f: A \to B$	\$f\colon A\rightarrow B\$
L(a, b; c; x, y; z)	\$L(a,b;c\colon x,y;z)\$

Plain T_EX also defines \ldotp and \cdotp to be '.' and '.' with the spacing of commas and semicolons. These symbols don't occur directly in formulas, but they are useful in the definition of \ldots and \cdots.

14. Alternate names. If you don't like plain T_EX 's name for some math symbol for example, if there's another name that looks better or that you can remember more easily—the remedy is simple: You just say, e.g., '\let\cupcap=\asymp'. Then you can type 'f(n)\cupcap n' instead of 'f(n)\asymp n'.

Some symbols have alternate names that are so commonly used that plain TFX provides two or more equivalent control sequences:

<mark>≠ \ne</mark> or \neq	(same as \not=)
<pre></pre>	(same as \leq)
<mark>≥ ∖ge</mark>	(same as \geq)
{ \{	(same as \lbrace)
} \}	$(same as \rbrace)$
\rightarrow \to	(same as \rightarrow)
$\leftarrow \ \texttt{\gets}$	(same as \leftarrow)
\ni \owns	(same as \ni)
\land \land	(same as \wedge)
∨ \lor	(same as \vee)
\neg \lnot	(same as \neg)
\vert	(same as)
∥ \Vert	(same as \downarrow)

There's also $iff (\iff)$, which is just like Longleftrightarrow except that it puts an extra thick space at each side.

15. Non-math symbols. Plain $T_{E}X$ makes four special symbols available outside of math mode, although the characters themselves are actually typeset from the math symbols font:

§ \S
¶ \P
† \dag
‡ \ddag

These control sequences do not act like ordinary math symbols; they don't change their size when they appear in subscripts or superscripts, and you must say, e.g.,

colon colon ldotpcdotp ldots cdots ne neq le ge to gets owns land lor lnot

vert iff