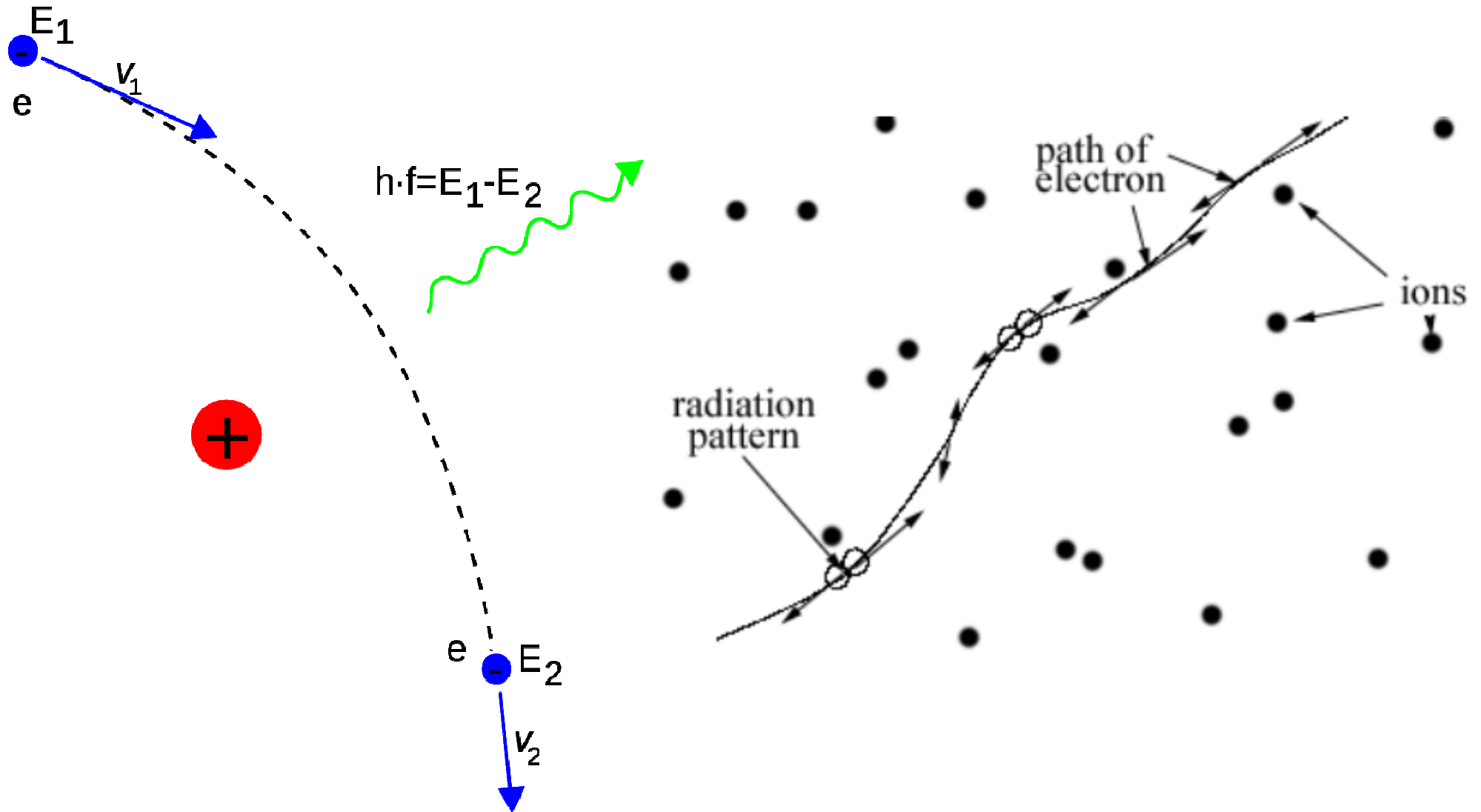


Bremsstrahlung



Thin-target Bremsstrahlung:

incident electron distribution is nearly unchanged, evolves slowly under the influence of collisions

Thick-target Bremsstrahlung:

incident electrons are completely stopped or thermalized in the high-density target

substantial change in incident electron distribution

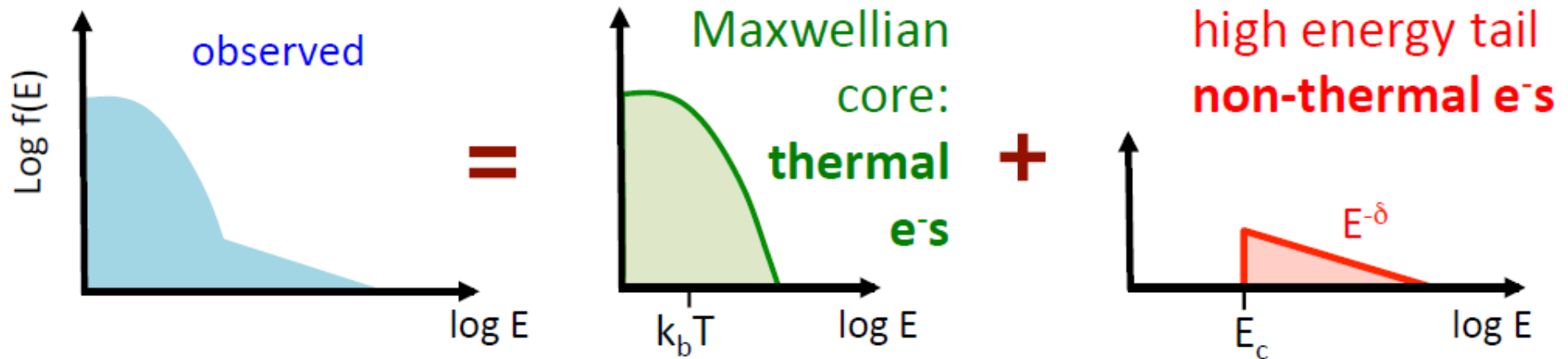
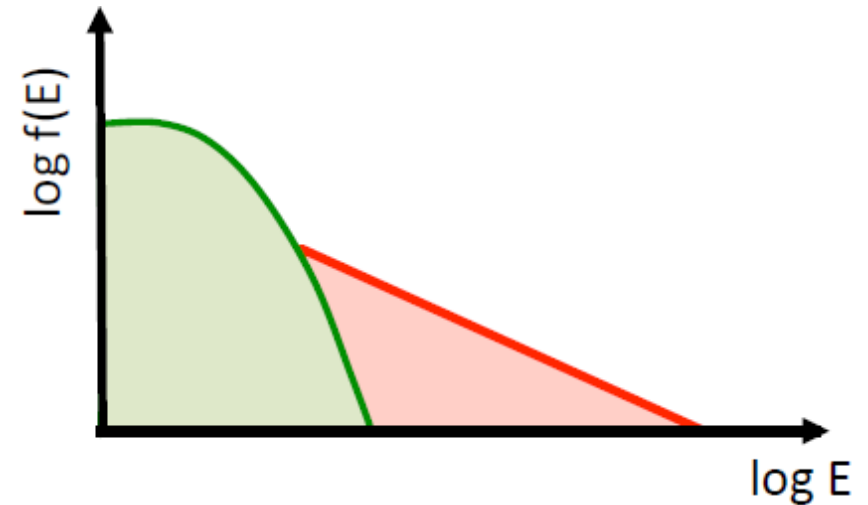
much quicker energy loss from electrons → lots of X-ray photons emitted → intense X-ray emissions (~10 keV-300 keV)

The photon flux emitted per unit energy observed at a distance R is obtained by integrating over the emitting source volume V or, for an imaged source, along the line-of-sight through the source region.

Collision rate scales inversely with energy.
 Collisions "relax" distribution toward a Maxwellian.

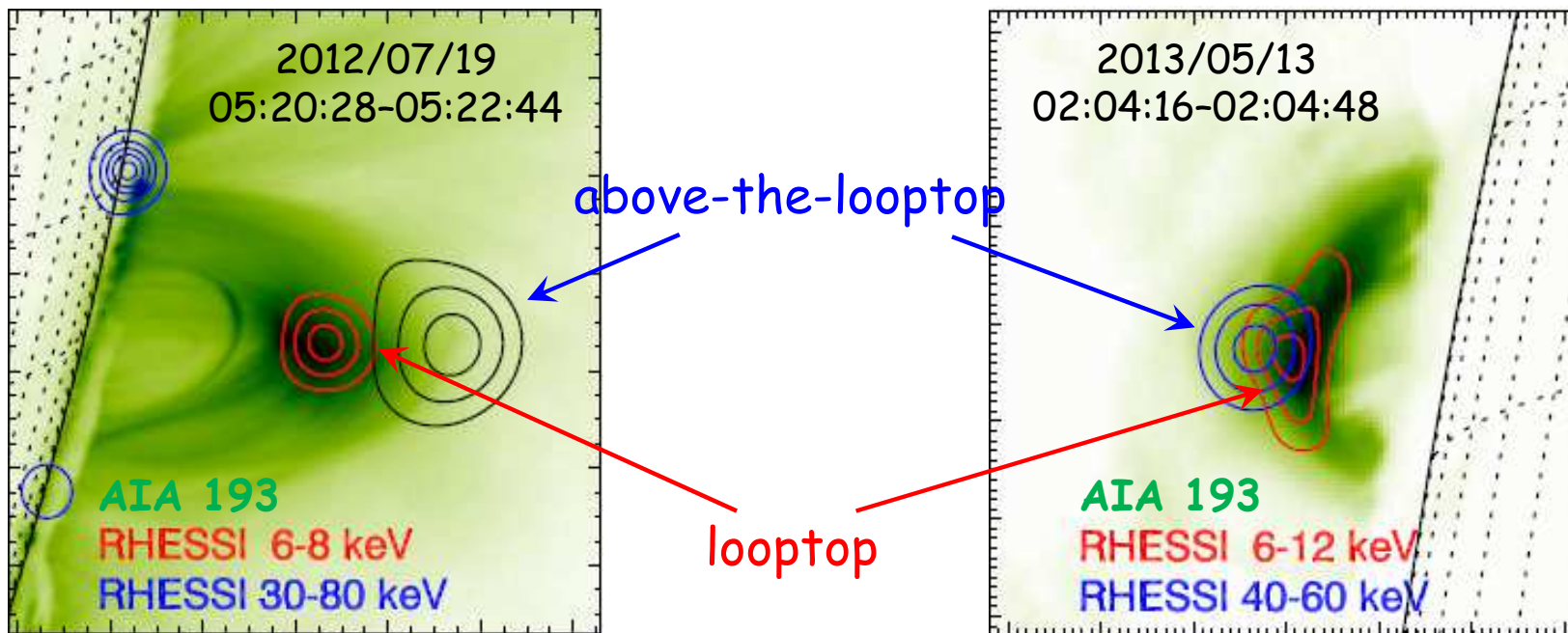
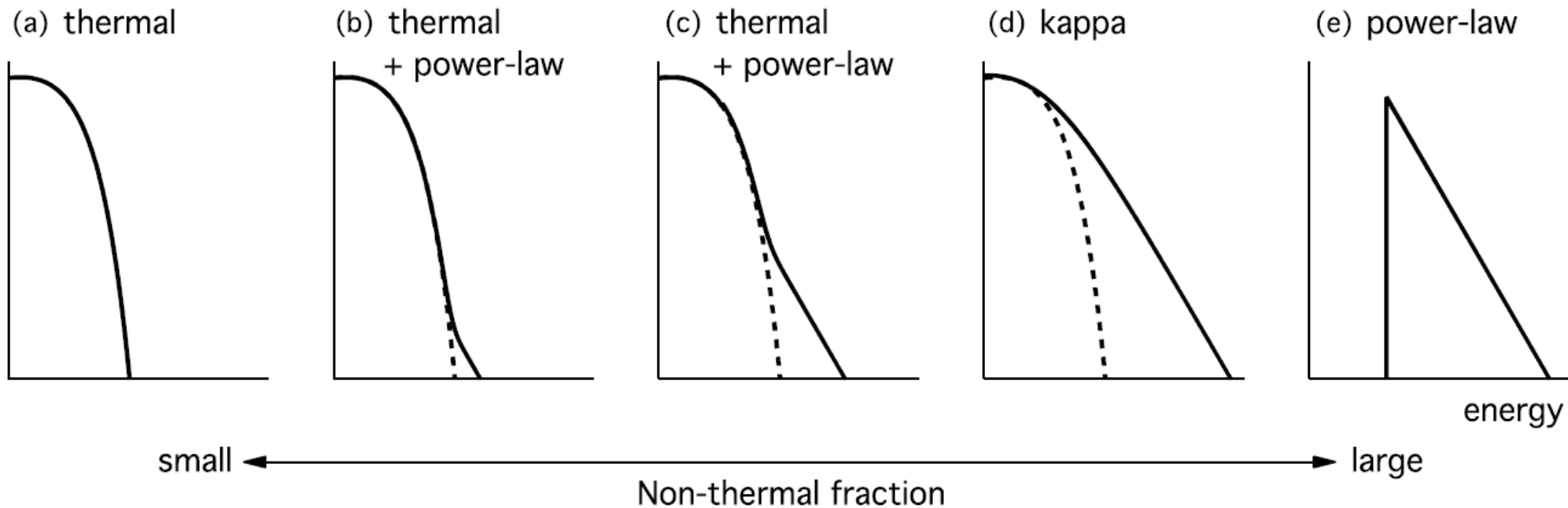
Low energy particles relax quickly
 → **Maxwellian core**

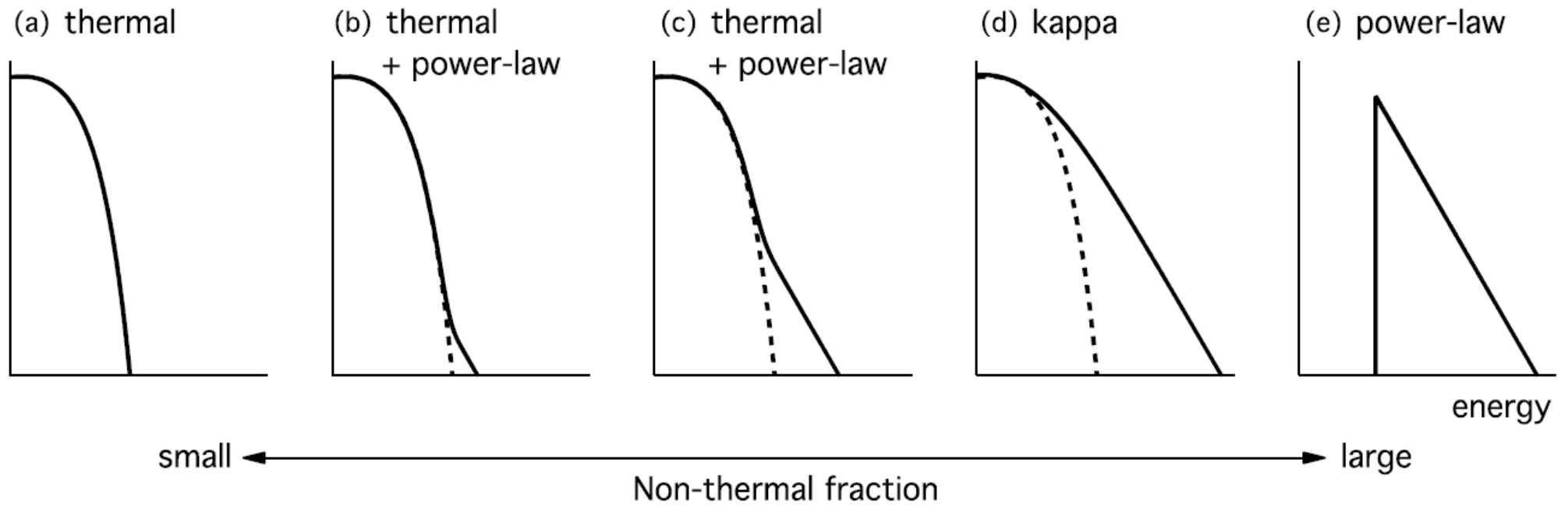
High energy particles fail to relax
 → **tail**



Radiation from a Maxwellian particle distribution is referred to as thermal radiation.

Radiation from a non-Maxwellian particle distribution is referred to as nonthermal radiation.





Thermal (Maxwellian):

$$F_M(E) = \frac{2N_M\sqrt{E}}{\sqrt{\pi}(k_B T_M)^3} \exp\left(-\frac{E}{k_B T_M}\right)$$

Power-law:

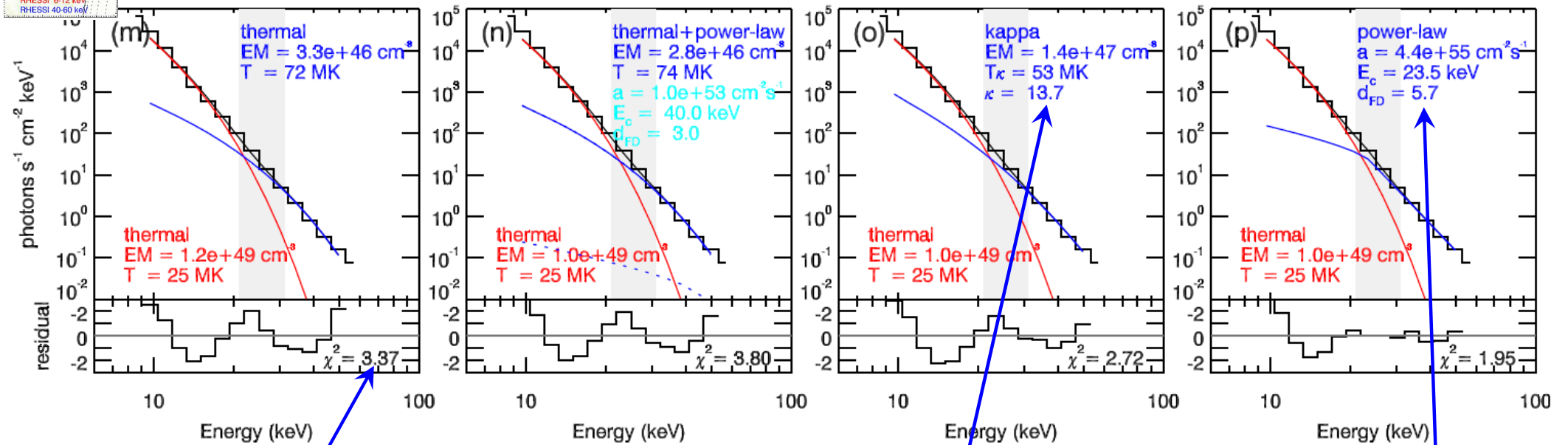
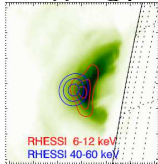
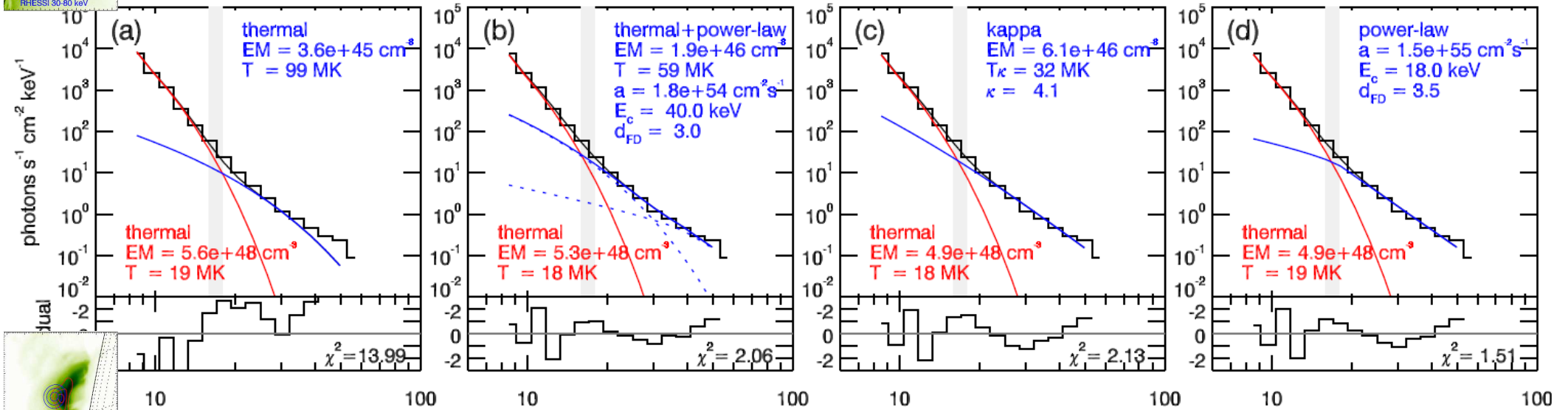
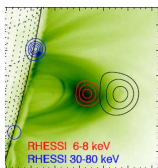
$$F_{PL}(E) = N_{PL}(\delta - 1)E_c^{\delta-1}E^{-\delta} \quad (\text{for } E \geq E_c)$$

Kappa:

$$F_\kappa(E) = \frac{2N_\kappa\sqrt{E}}{\sqrt{\pi}(k_B T_\kappa)^3} \frac{\Gamma(\kappa + 1)}{(\kappa - 3/2)^{3/2} \Gamma(\kappa - 1/2)} \left[1 + \frac{E}{k_B T_\kappa(\kappa - 3/2)}\right]^{-(\kappa+1)}$$

F: differential density ($\text{cm}^{-3} \text{keV}^{-1}$)
 E: particle energy
 N: number density
 T: temperature,
 E_c : lower-energy cutoff
 δ and κ : power-law indices
 Γ : Gamma function

The thermal+power-law model systematically overestimates and underestimates the temperature and density, respectively, due to the lower-energy cutoff E_c .



less enhanced nonthermal tail

close to Maxwellian

less significant nonthermal component

$F(E,r)$: electron flux density distribution
electrons $\text{cm}^{-2} \text{s}^{-1} \text{keV}^{-1}$

$F(E)$: electron flux distribution
electrons $\text{s}^{-1} \text{keV}^{-1}$

$f(E,r)$: electron density distribution
electrons $\text{cm}^{-3} \text{keV}^{-1}$

$$F(E,r) = f(E,r)v(E)$$

assume $F(E,r) \propto E^{-\delta}$, $f(E,r) \propto E^{-\delta'}$

$$\gamma_{\text{thin}} = \delta + 1, \gamma_{\text{thick}} = \delta - 1$$

$$\gamma_{\text{thin}} = \delta' + 0.5, \gamma_{\text{thick}} = \delta' - 1.5$$